

**THE ECONOMIC INFLUENCE OF  
INFRASTRUCTURAL EXPENDITURE: A  
MULTIPLIER DECOMPOSITION AND  
STRUCTURAL PATH ANALYSIS**

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April 2009



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**centre for poverty employment and growth**

## Human Sciences Research Council

April 2009

### ***Acknowledgments***

*This paper is a contribution to the HSRC employment scenarios and the dti's 'employment in the critical path' programme. This is a collaborative programme which seeks to identify innovative approaches to putting employment centre-stage of development strategy. The papers produced in this series are focused on identifying the pattern of employment creation within the growth/development path. We are grateful for the financial support of the dti.*

*We would also like to thank Rob Davies and Miriam Altman for their comments and contribution.*

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## Abbreviation List

### Production Activities

CAGRI	Agriculture
CCOAL	Coal
CGOLD	Gold
COTHM	Other mining
CFOOD	Food processing
CBEVT	Beverages and tobacco
CTEXT	Textiles
CAPPA	Wearing apparel
CLEAT	Leather products
CFOOT	Footwear
CWOOD	Wood products
CPAPR	Paper products
CPRNT	Printing and publishing
CPETR	Petroleum products
CBCHM	Chemical products
COCHM	Other chemical products
CRUBB	Rubber products
CPLAS	Plastic products
CGLAS	Glass products
CNMMP	Non-metallic metal products
CIRON	Basic iron and steel
CNFRM	Non-ferrous metals
CMETP	Metal products
CMACH	Machinery
CELMA	Electrical machinery
CCOME	Communication equipment
CSCIE	Scientific equipment
CVEHI	Vehicles
CTRNE	Transport equipment
CFURN	Furniture
COTHI	Other industries
CELEG	Electricity and gas
CWATR	Water
CCONS	Construction
CTRAD	Trade services
CHCAT	Hotels and catering
CTRAN	Transport services
CCOMM	Communication services
CFINS	Financial and real estate services
CBUSS	Business services
CMAOS	Medical and other services
COTHP	Other producers
CGOVS	Government services
DTCTRM	Import marketing margins
DTCTRE	Export marketing margins
DTCTRD	Domestic marketing margins

### Factors

FLABHI	Labour - high skill
FLABLS	Labour - low skill
FLABSK	Labour – skilled
FCAP	Capital

### Households

HENTRP	Enterprises
HHDLLOW	Household - income decile 00-50
HHDMID	Household - income decile 50-90
HHDWHI	Household - income decile 90-100

## **Abstract**

This paper is the result of a project that developed structural path analysis (SPA) as a tool for policy analysis. Using the planned infrastructural program, this paper demonstrates one of the many applications of SPA in answering a broad range of policy questions. The construction sector in South Africa is expected to play an important role in the upcoming years. This is especially so in the context of a global economy that is facing one of the worst downturns in world economic history. South Africa's GDP is expected to contract in 2009. The mining and manufacturing sectors are already adjusting for a decline in input and consumer demand. A R787 billion infrastructure investment program has been put in place and is viewed as a key component to promoting economic growth. The analysis indicates that the construction sector appears to be an excellent choice for a significant demand injection as it is large enough to accommodate a substantial stimulus and it also has significant linkages with nearly all other production activities and households at all income levels. The structural path analysis allowed us to get a better understanding of the sectorial composition of output, employment and household income. We were able to see which poles (production sectors, factors and households) are important transmitters of economic influence. Within the production sectors, business services, non-metallic metal products, mining and metal products are some of the most important sectors through which economic influence is transmitted to households via factor payments. Due to the economic downturn, most of these sectors are likely to be characterized by significant excess capacity. This implies that a demand injection into construction for infrastructure spending may be particularly well directed in terms of a stimulus to aggregate demand. The benefits of this intervention, with a few exceptions are distributed relatively evenly across the economy. Our results indicate that the planned infrastructure programme has the potential to significantly offset the contractionary effects of the global downturn. From the results it is clear that a "large" infrastructural investment program is highly recommended. Though our analysis does not say anything about the size of such an investment, the proposed R787 billion government infrastructural program is more than sufficient to generate the desired stimulus in the economy given the size of the multipliers in the construction sector and the paths through which its economic influence is transmitted throughout the economy. SPA provides policymakers with a tool that allows quick analysis of a given intervention based on the simple structural relationships of the economy built into the social accounting matrix.

## 1. Introduction

During 2008, South Africa's economy grew by 3.1%. This growth was below the estimated 3.7% due to poor performances during the third and fourth quarters (during the last quarter of 2008 GDP contracted by 1.8%). The global decline in the demand of raw materials has hit South Africa hard. In 2009, the economy is expected to contract, like in many other countries worldwide. The manufacturing and mining sectors have experienced particularly sharp declines. Overall, companies downscaled their production activities and capacity during the first quarter of 2009.

In response to the downturn, an infrastructure investment program is planned. It is hoped that the construction sector and other infrastructure related sectors will play an important role in boosting the South African economy. Specifically, the government plans on spending R787 billion on infrastructural investments over the next 3 years. The funds will be used for public transport, roads and rail networks; school buildings, clinics and other provincial infrastructure projects as well as municipal infrastructure and bulk water systems. In addition, Eskom and Transnet will get a large portion of the planned expenditure. A final allocation will support preparations for the 2010 World Cup.

We analyse the economic impact of the planned infrastructural investment program on the South African economy. In conducting this analysis, we hope to shed light on the mechanisms through which the infrastructural spending will stimulate the economy. In addition, we hope to develop and strengthen the use of Structural Path Analysis (SPA) as a tool for policy analysis in South Africa. The chosen topic demonstrates the usefulness of SPA framework. We believe that SPA can provide timely responses to policy questions on a range of issues.

The hypothesis underlying SPA, as Roberts (2005) points out, is that different sectors will be more or less important as 'connections' for transmitting influence between accounts in the economic system depending on the combination of expenditure patterns, and sourcing of inputs. This analysis focuses on the construction sector, which is the most likely to benefit directly from the increase in infrastructural expenditure. The distributional and employment impacts are also discussed.

The analysis seeks to provide answers to the following questions:

- Which sectors play an important role in the transmission of influence in the economy following an increase in infrastructural expenditure?
- The additional employment, by skill group, occurs in which sectors following an increase in the demand for construction services?
- Which other sectors in the economy are the primary beneficiaries of an increase in the demand for construction?
- How does this intervention affect the sectoral distribution of employment?
- And which household groups benefit the most?

## **2. Literature review**

### **2.1. The importance of infrastructure expenditure**

The provision of infrastructure confers a number of benefits to an economy. Infrastructure lowers the cost of production and consumption, and makes it easier for participants in the economy to enter into transactions. Increasing the efficiency of infrastructure will thus improve growth performance, service provision and development outcomes<sup>1</sup>. The importance of infrastructure is highlighted by Heymans and Thome-Erasmus (1998) who stress that the availability or absence of the 'right' infrastructure often affects the decisions producers and consumers about where to live or work, what to produce and also whether to produce. This in turn affects the ability of the economy as a whole to adjust to changes and external shocks. Most infrastructure has a fixed location. To use it, producers and consumers must be in the same place as the infrastructure facility. The availability of different types of infrastructure in a particular area often leads to agglomeration of economic activity in regions, cities and other localities. This results in enhanced production, consumption and trade. Given the importance and the role that this spending is going to have on the South African economy, it is natural to try and find out what influence the infrastructure program is going to have on the economy.

### **2.2. Empirical evidence**

The application of the SPA decomposition has been relatively rare, and as such, this review will concentrate on the few papers that have been published to date. Roberts (2005) illustrated how SPA can be used to analyze the role of different types of households in rural economies. To be specific, she showed the extent to which different types of households transmit economic influence or act as connections within the local economic system. Her study was on a rural region of Scotland – the Western Isles. This region has several rural development problems such as lagging per capita GDP, large trade deficits and a declining and aging population. In her analysis, the agricultural sector was selected as the origin account for each of the micro-level examples of path analysis. Each of the examples focused on the effects arising from a unit increase in demand for output from agriculture for another productive sector (the destination account). The three destination sectors were the banking, extraction and catering sectors, which were selected to illustrate the variety in the kind of paths that exist within the economy. Some indirect paths were shown to be more important than more direct paths because of the amplifying effect of adjacent circuits. Specifically, paths including the household accounts exhibited far higher multipliers than those contained within the production sphere of the economy. Furthermore, households with children were shown to play a more important role in generating the overall global influence than households with no children or retired households. Finally,

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<sup>1</sup> Heymans and Thome-Erasmus (1998)



‘other income’ was shown to be the most important factor of production. This is not surprising, given that self-employment income as opposed to salaried employment dominates agriculture in the region and thus acts as the main transmitter of influence into the household sector.

Khan and Thorbecke (1989) also used SPA to analyze the macroeconomic effects of technology choice on output, employment and income distribution. This was done by looking at the impact of the gradual substitution of traditional technologies by modern technologies in Indonesia. The path analysis was able to reveal the entire network of paths through which the impact of a particular technology was transmitted to the disaggregated socioeconomic system. The multiplier decomposition exercise showed that an increase of 100 Rupiahs into the hand-pounded rice activity (traditional technology sector) led to an increase of 22 Rupiah in the income of agricultural employees. The path analysis went on to reveal that 44.1% of the additional income to agricultural employees followed a path consisting of three consecutive arcs from hand-pounded rice to other food crops, to income accruing to the labour group “agricultural paid rural workers” involved in paddy production to income of the household group headed by agricultural employees. In this case, the latter indirect path was greater than the direct contribution of hand-pounded rice to agricultural employees. This is a good example of some of the benefits of using SPA over conventional decomposition methods.

### **3. Methodology**

Multiplier analysis is used to identify key sectors within an economy, particularly those that have the potential for generating high demand-led multiplier effects. The importance of a sector is based on the column sums of particular rows of the multiplier matrix from a closed input – output or SAM (Social Account Matrix) model. Sectoral multipliers are useful for considering the economy-wide impacts arising from exogenous increases in sector income.

Multiplier analysis can be complemented by multiplier decompositions and Structural Path Analysis (SPA). Multiplier decompositions are developed formally below. They allow for an additive decomposition of effects. SPA focuses on how individual elements lead to the global influence that we get from conventional SAM based decompositions by tracing the transmission of influence within an economic structure. It is a means of identifying the paths through which structural relationships in an economy lead to ultimate effects on endogenous variables. SPA reveals aspects of an economy that are not apparent from an examination of either direct transactions between accounts or an examination of the global influence which is the solution of conventional decompositions.<sup>2</sup>

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<sup>2</sup> Roberts (2005)

Structural path analysis has two key objectives;

- 1) To identify the most important interactions or paths within an economic system
- 2) To identify which individual poles (sectors, factors or households) are important transmitters of economic influence.

SPA is designed to provide a more detailed picture of the effects of shocks to exogenous accounts. SAM-multipliers measure the cumulative effects from a shock, while the path analysis decomposes these multipliers into direct and indirect components. The SPA decomposition is, in this context, useful in coming to grips with the nature and strength of linkages that work through the economic sector. Multiplier analysis, multiplier decompositions, and structural path analysis are attractive methodologies that can help provide insights into a range of policy questions around government's employment targets, stimulus policy, issues related to industrial policy and many other policy questions.

In comparison to CGE models, SAM multiplier analysis has several advantages. The first is simplicity. The multipliers are easy to calculate and their presence allows us to easily rank sectors by strength of overall stimulating impact. SPA is somewhat more complex. It goes further allowing us to rank paths of influence. We can also quantify the direct influence, the path multiplier and the total influence. CGE models are still more complex. The results of a CGE model are closely linked to the specification of the experiment, the choice of behavioral parameters, and the assumptions that are used to close the model. The flexibility of CGE models can result in controversy over appropriate choices. SPA as a technique involves applying a set of mathematical formulas to a SAM and then pulling out the multipliers and decomposing them with the goal of helping us better to understand economic interlinkages.

### **3.1. Multiplier Decomposition**

This project uses the 2003 SAM for South Africa (Table 1), which is the most recent accurate and consistent SAM available. A SAM provides a detailed snapshot of the economy at a point in time. Unlike input-output analysis, multiplier analysis in a SAM framework permits incorporation of feedback effects from household consumption. In addition, the detailed representation of households present in the 2003 SAM allows one to consider the distributional impacts of various types of demand injections. Some comments on the household disaggregation in the SAM are provided in Annex A.

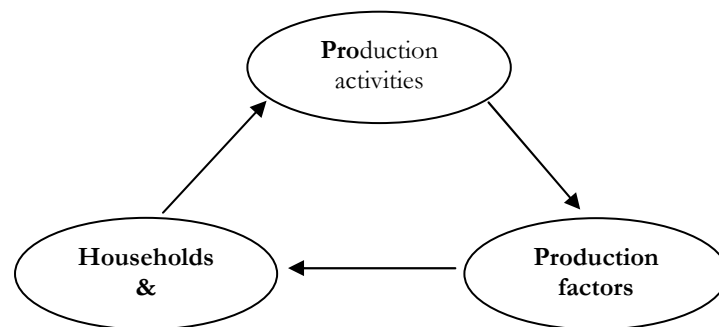
Using the 2003 SAM, we can measure the effects of various exogenous injections into the South African economy via multiplier decomposition and structural path analysis. In the next two subsections, we explain what each of these two methods encompass. However, before proceeding, it is important to highlight the limitations of multiplier analysis. Because multiplier decomposition and SPA are means of comprehending in greater detail the implications of the multipliers, they share these limitations.

In order for the results of multiplier analysis to strictly apply to the economy, two important assumptions must hold simultaneously. First, supply side constraints to economic expansion are not binding. As a result, the level of demand determines the level of economic activity. Second, one must either assume that prices are constant or that preferences and technology are of the Leontief form. In other words, consumers consume in fixed proportions and producers use inputs in fixed proportions either because fixed relative prices provide no incentives to change those proportions or because preferences and technology are specified in that way.

Ordinarily, these assumptions are considered highly onerous. Multiplier analysis is often viewed as providing useful insights into demand forces on the economy that may be important for the nature and rate of economic growth; however, the interpretation of results is usually tempered by a more realistic view of supply side, prices, preferences, and technology. However, in the context of the current economic downturn, the assumptions behind multiplier become more plausible. With economic contraction in process, supply side constraints are clearly less problematic. At the same time, while prices, preferences, and technology almost surely maintain some flexibility, fixed proportions preferences and technology provide a valuable first order approximation to the effects of demand shifts within the South African economy.

The 2003 SAM includes a total of 73 accounts, which can be divided into endogenous and exogenous accounts. The endogenous accounts include 46 commodities, 4 factors, and 15 institutions (enterprises and households). On the other hand, the exogenous accounts include 4 types of taxes, government, savings-investment balance, changes in stocks, and the rest of the world. In a multiplier decomposition, as proposed by Pyatt and Round (1979) and Defourny and Thorbecke (1984), the effect of injections from exogenous accounts can be tracked on the economy (endogenous accounts). Under the assumptions mentioned above (fixed prices and no supply restrictions), multiplier decomposition can reveal the interaction between and across the categories shown in Figure 1.

**Figure 1 – Interrelationship among SAM Categories**



*Source: Adapted from Defourny and Thorbecke (1984)*

Figure 1 represents the triad that disciplines the flow of expenditure within the economic system. Expenditure flows from production activities to factors of production as factor payments. These are then mapped on to households as household income and this income is then used to purchase goods and services from

production activities completing the circular flow of income. SPA is also conditioned by this relationship, in other words when choosing the poles of analysis it is not possible to have a direct flow from production activities to households.

The multiplier decomposition method presented here draws heavily on the work by Pyatt and Round (1979), Defourny and Thorbecke (1984), and Stone (1985). Multiplier decomposition is concerned not only with output levels and the level of factor and household incomes, but also with the structure of production, the distribution of factor incomes, and the distribution of disposable income both among households and between them and enterprises (Pyatt and Round, 1979).

Initially, the SAM ( $S$ ) is partitioned into endogenous and exogenous accounts. The endogenous accounts include production activities ( $a$ ), factors ( $f$ ), and institutions ( $i$ ) (enterprises and households). On the other hand, the exogenous accounts ( $x$ ) include the government, capital, and the rest of the world.

$$(1) \quad S = \begin{bmatrix} S_{aa} & S_{af} & S_{ai} & S_{ax} \\ S_{fa} & S_{ff} & S_{fi} & S_{fx} \\ S_{ia} & S_{if} & S_{ii} & S_{ix} \\ S_{xa} & S_{xf} & S_{xi} & S_{xx} \end{bmatrix}$$

Once the SAM has been partitioned, average expenditure shares for each column are calculated. Submatrix ( $A_n$ ) only includes endogenous accounts.

$$(2) \quad A_n = \begin{bmatrix} A_{aa} & A_{af} & A_{ai} \\ A_{fa} & A_{ff} & A_{fi} \\ A_{ia} & A_{if} & A_{ii} \end{bmatrix}$$

With this matrix, the accounting multiplier matrix can be obtained.

$$(3) \quad M_a = (I - A_n)^{-1}$$

Matrix  $A_n$  is then decomposed into Matrixes B and C.

$$(4a) \quad A_n = \begin{bmatrix} A_{aa} & A_{af} & A_{ai} \\ A_{fa} & A_{ff} & A_{fi} \\ A_{ia} & A_{if} & A_{ii} \end{bmatrix} = \begin{bmatrix} A_{aa} & 0 & 0 \\ 0 & A_{ff} & 0 \\ 0 & 0 & A_{ii} \end{bmatrix} + \begin{bmatrix} 0 & A_{af} & A_{ai} \\ A_{fa} & 0 & A_{fi} \\ A_{ia} & A_{if} & 0 \end{bmatrix}$$

$$(4b) \quad A_n = B + C$$

Matrix B is the partition which includes all the interactions within each group of endogenous accounts (activities, factors, and institutions), and matrix C includes the coefficients of interactions across groups of endogenous accounts.

If we denote the vector of totals of all the endogenous accounts by  $y$  and the vector of the sums of the income elements into these accounts from all the exogenous accounts by  $x$ , then:

$$\begin{aligned}
 (5) \quad \mathbf{y} &= \mathbf{A}\mathbf{y} + \mathbf{x} \\
 &= \mathbf{B}\mathbf{y} + \mathbf{C}\mathbf{y} + \mathbf{x} \\
 &= (\mathbf{I} - \mathbf{B})^{-1}\mathbf{C}\mathbf{y} + (\mathbf{I} - \mathbf{B})^{-1}\mathbf{x} \\
 &= [[\mathbf{I} - (\mathbf{I} - \mathbf{B})]^{-1}\mathbf{C}]^{-1} (\mathbf{I} - \mathbf{B})^{-1}\mathbf{x} \\
 &= (\mathbf{I} - \mathbf{D})^{-1}(\mathbf{I} - \mathbf{B})^{-1}\mathbf{x} \\
 &= (\mathbf{I} + \mathbf{D})(\mathbf{I} - \mathbf{D}^2)^{-1}(\mathbf{I} - \mathbf{B})^{-1}\mathbf{x} \\
 &= \mathbf{M}_3\mathbf{M}_2\mathbf{M}_1\mathbf{x} \\
 &= \mathbf{M}_a\mathbf{x}
 \end{aligned}$$

where  $\mathbf{D} = (\mathbf{I} - \mathbf{B})^{-1}\mathbf{C}$

From equation (5), the accounting multiplier is decomposed into Matrixes  $\mathbf{M}_1$ ,  $\mathbf{M}_2$ , and  $\mathbf{M}_3$ .

$\mathbf{M}_1$  captures the within account effects, which is the multiplier effect into a category (production activities, factors, or households). For the production activities sector,  $\mathbf{M}_1$  represents the input-output multiplier.

$$(6) \quad \mathbf{M}_1 = (\mathbf{I} - \mathbf{B})^{-1}$$

$\mathbf{M}_2$  captures the cross/spillover effects, where the injection into a category has an effect on another category with no reverse effects.

$$(7) \quad \mathbf{M}_2 = (\mathbf{I} + \mathbf{D} + \mathbf{D}^2)$$

Lastly,  $\mathbf{M}_3$  captures the between effects net of the within-account multipliers.  $\mathbf{M}_3$  shows the full circular effect.

$$(8) \quad \mathbf{M}_3 = (\mathbf{I} - \mathbf{D}^3)^{-1}$$

As  $\mathbf{M}_1$ ,  $\mathbf{M}_2$ , and  $\mathbf{M}_3$  enter the decomposition in a multiplicative fashion,  $\mathbf{M}_a$  is better expressed and understood in terms of additive components.

$$(9) \quad \mathbf{M}_a = \mathbf{I} + (\mathbf{M}_1 - \mathbf{I}) + (\mathbf{M}_2 - \mathbf{I})\mathbf{M}_1 + (\mathbf{M}_3 - \mathbf{I})\mathbf{M}_2\mathbf{M}_1$$

where  $\mathbf{I}$  is a matrix of injections. Equation (9) satisfies

$$(10) \quad \mathbf{M}_a = \mathbf{N}_1 + \mathbf{N}_2 + \mathbf{N}_3$$

$\mathbf{N}_1$  represents the own-effects. It captures the within category effects, including the direct effects from an increase in exogenous demand and the interaction effects within categories (activities, factors, or households). The submatrix that only includes activities is the same as the Leontief inverse of the input-output table.

$$(11) \quad \mathbf{N}_1 = \mathbf{M}_1$$

$\mathbf{N}_2$  represents the incremental open loop linkages. It captures the between effects of endogenous variables and the resulting within category effects. It includes the effects from additional demand across categories. Additionally, it includes the indirect effect within categories

$$(12) \quad \mathbf{N}_2 = \mathbf{Q}\mathbf{M}_2 - \mathbf{D}\mathbf{M}_1$$

$\mathbf{N}_3$  represents the closed loop effects. It captures the additional feedback effects, which were not included, as  $\mathbf{N}_2$  only included within categories indirect effects.

$$(13) \quad \mathbf{N}_3 = \mathbf{Q}\mathbf{M}_3 - \mathbf{D}\mathbf{M}_2\mathbf{M}_1$$

$\mathbf{N}_1$  and  $\mathbf{N}_2$  together represent the part of the multiplier effects from exogenous demand increases and the adjacent spill-over into other categories.  $\mathbf{N}_3$  represents the importance of the market for intermediate goods.

## 3.2. Structural Path Analysis

While the SAM multipliers measure the cumulative effects from an exogenous injection, the structural path analysis decomposes these multipliers and tracks the movement of a given injection across specific endogenous accounts.

Structural path analysis was developed by Defourny and Thorbecke (1984) based on the concepts of economic influence and structural analysis from Lantmer (1974) and Gazon (1976 and 1979). The following sections draw heavily on Defourny and Thorbecke (1984).

The building blocks of structural path analysis are the average expenditure propensities  $a_{ij}$  (which come from matrix  $\mathcal{A}$ ). They reflect the intensity of arc  $(i,j)$ . The intensity that links two poles of the structure and oriented in the direction of the expenditure is to be interpreted as the magnitude of the influence transmitted from pole  $i$  to pole  $j$ . There are three types of influence: direct, total and global.

### 3.2.1. Direct influence

The direct influence of  $i$  on  $j$  is only the change of  $j$  induced by a unitary change in  $i$ . This influence can be measured along an arc (14) or along an elementary path  $p$  (15).

$$(14) \quad \mathbf{I}_{i \rightarrow j}^p = \mathbf{a}_{ij}$$

$$(15) \quad \mathbf{I}_{(i \rightarrow j)_p}^D = \mathbf{a}_{jn} \dots \mathbf{a}_{m1}$$

### 3.2.2. Total influence

Using the concept of total influence developed by Lantner (1974), the indirect effects within the structural path can be identified. These indirect effects induced by the adjacent circuits amplify the direct influence in the elementary path.

$$(16) \quad \mathbf{I}_{(i \rightarrow j)_p}^T = \mathbf{I}_{(i \rightarrow j)_p}^D \mathbf{M}_p$$

where  $\mathbf{I}_{(i \rightarrow j)_p}^D$  is the direct influence along path  $p$  and  $\mathbf{M}_p$  the path multiplier. The path multiplier captures the indirect effects on adjacent feedback circuits.

$$(17) \quad \mathbf{M}_{p(ji)} = \frac{\Delta_p(ji)}{\Delta}$$

where  $\Delta$  is the determinant of the matrix  $(I - A)$  and  $\Delta_p(ji)$  is the determinant of the structure excluding the poles (both rows and columns) constituting path  $p$ .

### 3.2.3. Global influence

Global influence measures the total effects on income or output of the destination pole  $j$  consequent to an injection of one unit of output or income in the origin pole  $i$ . Global influence corresponds to the  $j,i$  element of the accounting multiplier matrix  $\mathbf{M}_a$  (3).

Global influence accounts for all direct and indirect influences transmitted by all elementary paths linking the origin and destination poles. Thus, the global influence can be decomposed into the total influences transmitted along all elementary paths between the origin and destination.

$$(18) \quad \mathbf{I}_{(i \rightarrow j)_p}^G = \sum_{p=n}^{\Pi} \mathbf{I}_{(i \rightarrow j)_p}^T = \sum_{p=n}^{\Pi} \mathbf{I}_{(i \rightarrow j)_p}^D \mathbf{M}_p$$

## 4. Results

### 4.1. Multipliers

Multiplier decomposition and structural path analysis provide the tools to assess the impact of an exogenous increase in the demand for construction in the South African economy. Our first step is to calculate the accounting multipliers (Table 2). These multipliers measure the global effect of an exogenous increase in the demand of a sector. When construction is stimulated via, for example, a government infrastructure investment program, demand for intermediate inputs used by construction expands. For example, construction is a significant user of non-mineral metal products. Non-mineral metal products, in turn, is both produced domestically and imported. In the multiplier analysis, the financial flows to imports and to taxes are examples of flows to exogenous accounts which are “leakages” from the system. Purchases of domestically produced non-mineral metal products remain within the system. The stimulus to the non-metal mineral products sector stimulates further intermediate demand for commodities.

At the same time, expansion of the construction sector requires increased use of factors of production—labour and capital. These resources are presumed to be unemployed and thus available to be used in the construction sector. In the South African case, unemployment of unskilled and semi-skilled labour has been a reality for decades. However, supply side constraints have been evident with respect to highly skilled labour and capital. Nevertheless, within the context of the current economic contraction, these constraints are likely to be far less binding. Increased factor income is distributed to households (with taxes and savings representing leakages). Household, in turn, expand consumption of commodities.

These internal loops persist resulting in a larger increase in aggregate demand than the initial stimulus into the construction sector. Assuming that the R787 billion infrastructure project over three years is entirely used in construction activities and the division of financing is roughly equal per year, the activity multiplier of nearly 5 implies that the initial increase will swell to nearly R1.3 trillion worth of sales as the secondary effects are felt throughout the South African economy. This means that a one unit increase in construction demand (via, for example, a government infrastructure investment program) results in nearly four additional units of sales in construction and other industries. Similarly, factor incomes (GDP at factor cost) expand by more than R333 billion and household incomes expand by nearly R250 billion on an annual basis.

These numbers are clearly too large in the context of an economy where GDP was valued at R1.26 trillion in 2003, which is the base year for the SAM.<sup>3</sup> This result

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<sup>3</sup> World Development Indicators (World Bank, 2009)



highlights the need for appropriate consideration of results. Nevertheless, the results show that expansion of the construction sector has considerable potential to provide demand side stimulus. To the extent that supply side constraints within the overall economy remain non-binding, the stimulus has potential to significantly push the economy towards the production possibilities frontier.

#### *4.1.1. Production activities*

The stimulus in the construction sector generates motion in all other productive activities. Within the productive activities, the largest sales stimulus (outside of construction) is received by the business services sector (0.52). Only one sector, furniture, provides a larger impetus to sales by domestic producers, with an activity multiplier over 5.

#### *4.1.2. Factors*

As mentioned above, the initial stimulus to construction also increases factor usage (capital and employment) and factor income. These factor earnings are then passed to households, though some of the incremental income leaks to factor taxes, corporate taxes, and retained earnings. The net result is that, even though value added represents only about 20% of total construction costs, the overall stimulus to factors (value added) amounts to 1.32 once all indirect effects are accounted for. The impact on total household income is less at 0.95 due to the leakages mentioned above. Retained earnings and corporate taxes are the main elements that account for the differences for two reasons. First, the construction sector is reasonably capital intensive with a share of capital in value added of 41%. While less than the economy-wide average capital intensity of 48%, the share still implies that significant payments are directed to capital. Second, these payments to capital are subject to corporate and factor taxes as well as retained earnings. These leakages represent nearly 50% of capital income.

#### *4.1.3. Institutions*

Given the resulting stimulus on all production activities, enterprises receive, directly and indirectly, a large portion (65%) of the investment from the infrastructure program. The households in the SAM were previously grouped by income deciles, with the first group representing households with incomes between the 0 and 10 percentile, and the last one for the household with incomes between 98.75 to 100 percentile. Nonetheless, by grouping these households into only three categories, the results can be more easily explained. The distribution was made as follows: low (0-50), medium (50-90), and high (90-100).

The distribution of benefits of augmented construction spending across households is not as favourable as one might like. The incomes of middle and upper income households each increase by 0.42 while lower income households benefit from a 0.11 stimulus. However, this is more a feature of the South African economy than of the construction sector. Relatively few sectors provide a greater stimulus to overall household income than construction and even fewer provide a larger stimulus to lower income households. The low multipliers for low income households reflect a high degree of dependence of these households on government transfers as a source of income. For households in the lower 50% of the income distribution, government

transfers represent a bit less than 33% of income. The small shares of factor earnings garnered by low income households imply relatively low multipliers for these households.

Overall, the multiplier effect of construction spending on factor incomes is generally strong relative to other sectors, though not as strong as with respect to activities. Sectors with larger shares of value added in total sales and higher labour intensities, such as government services, produce larger multipliers with respect to factor incomes. Nevertheless, the construction multiplier is relatively high.

## 4.2. Multiplier Decomposition

The total effects presented by the accounting multipliers can be decomposed as suggested in equations (11), (12), and (13). We divide the effects into two sets. The first one represents the part of the multiplier effects from exogenous demand increase and the adjacent spill-over into other categories (own and loop effects), while the second represents the additional feedback effects across categories (closed loop effects). Table 3 presents the own and loop effects as a share of total effects, while Table 4 the share of closed loop effects. The different composition between these sets can be explored by comparing the composition of the global effects of a demand increase on construction versus an increase on food processing. As expected, agriculture receives most of the benefits directly when the food processing sector is stimulated. Conversely, most of the benefits for agriculture come from indirect effects (74%) when the construction activities are stimulated.

### 4.2.1. Production activities

We can now decompose the effects observed in Table 2 for key sectors. The values in Table 3 for production activities are for own effects ( $N_i$ ). In the iron and steel sector, 80% of the income generated was through direct effects (within the activities category). Electricity and gas had 50%, as the indirect effects with other categories (factors and consequently, households) create an additional demand for electricity and gas. Aside from construction, the sector with the largest direct effect (98%) was gold. On the other hand, we can observe in Table 4 that sectors such as wearing apparel, agriculture, beverages and tobacco receive most of the benefits from closed loop effects as they are indirectly related to the construction sector.

### 4.2.2. Factors

In South Africa, the construction sector is a significant user of both capital and labour. The shares presented in Table 3 represent open loop effects ( $N_2$ ) only. This is due to the fact that open loop effects capture the effects that the infrastructure programme has on both factors and institutions (enterprises and households). More than half of the income received by factors comes from spillover effects, with low skilled labour receiving the largest share (75%). Capital, skilled labour, and high skilled labour receive a significant share of the generated income through closed loop effects.

#### *4.2.3. Institutions*

Last of all, we decompose the multipliers for both enterprises and households. As with factors, the values in Table 3 are from open loop effects ( $N_2$ ) only. More than half of the multipliers for low, medium, and high income households come from open loop effects. Low income households benefit more directly than other households, as most of their members are low skilled workers, which have a greater demand from the construction sector.

### **4.3. Structural Path Analysis**

This section presents the results of the SPA which goes a step further than the multiplier decomposition presented in the previous section. The previous multiplier decomposition gave us the global influences that exist between the construction sector and other poles (that is, production activities, factors, and institutions). Using structural path analysis, we now proceed to identify various paths, through which economic influence is transmitted from the construction sector (the pole of origin) to the other poles in the economy. The results for the structural path analysis in Tables 5 to 7 only show the ten most important paths in each case. These are not exhaustive since in any given SAM, there are thousands of possible paths.

#### *4.3.1. Production activities*

Table 5 shows the path analysis of construction on other production activities. Unlike conventional multiplier analysis SPA gives us the sectorial distribution of output following an intervention into a given sector. Case I in Table 5 shows the impact of such an injection in construction on basic iron and steel. Ordinary multiplier analysis only gives us the overall impacts, in this case it tells us that an injection of R1 billion into the construction sector generates an increase of R86 million in the income of basic iron and steel. Structural path analysis then shows us that only 27.1 % of this additional production is caused directly by the demand for basic iron and steel inputs by the construction sector through the path linking the two without any other sectors, households or factors. The other paths reveal that a significant part of the global influence of construction on basic iron is exercised indirectly through the metal products sector (33.1%) and this is actually greater than the direct influence. This means interventions should not simply be concerned with pouring money into a sector but should look at other sectors that contribute in delivering the influence of the targeted sector. Therefore policy should be more holistic in its approach and path analysis helps in identifying these important supporting sectors. This is not the case with conventional multiplier analysis which focuses on the global effects there by creating narrowly defined interventions. Path analysis therefore enables us to see exactly which sectors benefit by revealing the different paths through which economic influence is transmitted from construction to basic iron and steel. It can also be seen that the most important sector in transmitting this influence between the two sectors is the metal products sector since it appears in the 10 most significant paths between construction and basic iron and steel.

In Case V: Table 5, we see the paths between construction and the electricity and gas sector, the table indicates that the global influence of construction on the electricity and gas sector means that a R1 billion increase in the exogenous demand for construction output will lead to an estimated total increase in the value of electricity and gas output of R59 million. Twenty eight percent of this is as a result of the direct demand for electricity and gas from the construction sector itself. The path analysis reveals that there is a general increase in the demand for electricity from other sectors in the economy and that this increase is spread across activities, factors, and institutions. For example, the increase in the demand for non-metallic metal products represents 2.8% of the total increase. Households also increase their energy consumption. Low skilled households represent a larger share of the global influence, with 1.65% coming from medium income, 1.46% from low income households, while high skilled labour in high income households represents 0.89%.

Other paths that we consider are the ones with non-metallic metals and metal products as destinations. The construction sector spends about 11% of its budget on non-metallic metals. This activity benefits from a global influence of 0.16. Almost 95% is explained via a direct path. We also find sectors such as agriculture to play a role in this global influence, via a direct path between the two sectors. The global influence for metal products shows us that R1 billion invested in construction will lead to an increase of R119.5 million. Almost 75% of this comes from the direct path linking these two sectors. A smaller portion comes from indirect paths via the increased spending on iron, electrical machinery, and non-metallic products.

#### *4.3.2. Factors*

The increase in income following the exogenous expenditure on construction can be interpreted as a rise in the employment of the destination factor. Thus, with path analysis, we can establish the sectoral sources of additional employment following an increase in construction services. Conventional multiplier decomposition only tells us the overall impact without saying from which sectors the additional employment will come from and the problem with computable general equilibrium models is that the results depend greatly on the experiment being modeled and the rules used to close the model. This gives SPA a distinctive advantage over these techniques since it enables us get results based on the structural relationships within the SAM. Case II: Table 6 shows us the sectors where the additional employment of low skilled workers will come from following an increase in the expenditure on construction. It can be seen that 49% comes directly from the construction sector itself and the rest comes from other sectors, with non-metal products, other mining and gold being some of the top contributors to the increase in employment. The path analysis also shows that, out of the top 10 paths, other mining plays the most important role in transmitting the economic influence from construction to low skilled workers.

These are important results. The infrastructure program is expanding employment for unskilled workers in sectors that are suffering particularly weak demand in the context of the global economic contraction. This implies that, via this channel at least, the infrastructure program is likely to be effective in (at least partially) counteracting the slump in demand. In addition, the multiplier effects are less likely to encounter supply side constraints.

With respect to skilled and highly skilled labour, the business services sector stands out. The effect of the contraction on the demand for business services is less clear. Hence, constraints to the expansion of business services may limit the propagation of the demand injection from construction. Beyond business services, the sources of additional employment for skilled and high skilled labour seem to be evenly distributed without any one sector dominating as an important transmitter of influence. Specifically, the additional employment for high skilled labour comes from a more diverse combination of sectors. The construction sector spends about 9% of its budget on capital, and 13% on labour (5.6% on low skilled, 2.5% on skilled, and 4.5% on high skilled labour). We previously found that the construction sector has a multiplier effect of effect on capital, with a R1 billion injection in the construction sector generating almost R700 million of factor income. Path analysis shows us that the direct demand for capital by the construction sector represents only 21.3% of this total influence. The rest of the influence is transmitted indirectly through paths which flow past other production activities as the increase in capital income also comes from business services (5.9%), non-metallic metal products (4.5%), and metal products (1.09%), among others.

Low skilled labour has the highest budget share, but the lowest multiplier (0.16). On the other hand, high skilled labour has a relatively high multiplier (0.26). Almost half of the increase on low skilled labour income comes from its direct path with construction. Other sectors that employ additional units of labour are metal products, non-metallic metals, other metals, and gold. Conversely, business services, and financial and real estate services play an important role in the increase of high skilled labour income.

#### *4.3.3. Institutions*

Lastly, as in the case with labour, path analysis can also give us a better sense of the distribution of additional income for institutions (households and enterprises). Cases II, III and IV: Table 7 show us that the income of all households comes from a combination of diverse sectors; furthermore, path analysis tells us that the additional income of middle income households comes mainly from three sources: the business services, metal products and non-metal products sectors. This is revealed by the fact that these sectors appear an equal number of times in the paths that connect construction and middle income households. Path analysis also shows us that enterprises receive most of their income through the direct path via capital, which explains 21.3% of the total income generated (Case I: Table 6). The remaining share comes indirectly through capital but initially going from construction to business services (5.9%), non-metallic metal products (4.5%), other mining (2.27%) metal products (1.09%), and electricity and gas (0.93%), among others.

Low income households receive 23.2% of the income generated through low skilled labour, 5.6% from skilled, and 2.15% from high skilled labour. They also receive 4.36% of the income generated by construction, through capital invested in enterprises. Medium income households follow a similar pattern, but with a more even distribution among the paths explained above, where the income coming from low skilled labour represents 12.4% of the global influence. Last but not least, high income households receive 11.2% of their income from capital invested in enterprises, followed by 10.7% from high skilled labour. Production activities that consistently

participate in the paths of income generation for enterprises and households are non-metallic metal products, metallic products, and business services. These results show that South African households have relatively strong links to the industrial sector, and that many of the sectors involved in construction hire labour with different sets of skills.

#### 4.3.4. *A graphical representation*

The analyses presented above relied only on the quantitative results generated by SPA. Nonetheless, SPA is a construct of relationships within the economy and a graphical representation allows a potentially more straightforward interpretation of this construct. These figures showcase the 10 most important paths, with a maximum length of three arcs for Figures 1-3, and four paths for Figures 4-6. The thickness of the lines connecting the accounts represents the strength of the connection between the corresponding accounts. The thicker the line, the greater the relative volume of flow along the path. It is important to note that the thickness is not related to income magnitudes as the importance of the path also relates to both its influence and the path multiplier of adjacent circuits.

In Figure 1, we begin by looking at the movement of the influence generated by the injection in the construction sector. The four sectors below construction are sectors with paths connected to more than one factor. For example, metal production uses labour at all skill levels (together with construction), while business services mainly uses skilled and high skilled labour. Low skilled labour receives income from seven out of the ten production activities, and generates income for all households. High skilled labour is similarly benefited, whereas skilled labour is the least connected factor.

In order to put these relationships, created by an injection in the construction sector, into perspective, we also model in Figure 2, the effect from a direct injection in the production of electricity and gas, and in Figure 3 with respect to transport services. In the electricity and gas sector, we can observe that less production activities benefit in the top 10 paths. Business services do not have a strong effect on high skilled labour, and do not generate income for skilled labour, when compared to the construction case. The households with more connections in this case are middle income households. Lastly, with an injection in transport services, lower income households present strong ties to skilled labour. Skilled labour seems to be the most important factor, receiving their income from trade services, business services, transportation services, other producers, communication services, and transportation services. When comparing Figures 1, 2, and 3, we can see that an injection of income in construction generates much more activity than injections in either transport services or electricity and gas.

So as to better understand the distributional effects caused by the infrastructure programme, we generate three set of figures (showing up to four arcs) with corresponding effects on low income (Figure 4), middle income (Figure 5), and high income households (Figure 6). As expected, low income households benefit from stronger ties with low skilled workers. Nonetheless, they also receive income from enterprises. The skilled labour in low income households obtained their additional

income primarily from construction, and indirectly from financial services used by business services.

In the case of middle income households, there was a large flow between construction and business services, which in turn used financial services, capital, skilled and high skilled workers. Invested capital in enterprises created a lot of income activity with this household. Only four production activities are present in the top 10 paths, with business services being the most connected sector. This household enjoyed a more evenly distributed influence from all factors.

Our last figure showcases how income travels to high income households. These households are highly connected to enterprises and high skilled labour. The structure of this case resembles the one observed for middle income households, but with the other mining sector having greater importance and metal products no longer present. Enterprises in this case receive income from a greater number of activities including business services, non-metallic products, and other mining.

The results from the structural path analysis show that an infrastructure programme that generates income in the construction sector generates movement in a large number of production activities, factors, and institutions. The business services sector appears to be an important actor in this economy, together with non-metallic metal products. Income received by low income households comes from a very diverse set of activities, whereas high income households received capital rents from a larger set of activities, which is thereafter invested in enterprises.

#### *4.3.5. Discussion*

The results show that SPA is an important compliment to standard multiplier decomposition analysis and allows us to go beyond global effects. It allows us to get a better understanding of the sectorial composition of output, employment and household income. It also allows us to see which poles (production sectors, factors and households) are important transmitters of economic influence. As mentioned above unlike computable general equilibrium techniques that are better suited to counterfactual analysis and whose results depend heavily on the circumstances being modeled SPA provides policymakers with a tool that allows quick analysis of any intervention on the economy.

## 5. Conclusions

This paper analyzed the impact of the proposed infrastructure program using conventional multiplier decomposition and structural path analysis. Assuming that the R787 billion infrastructure project over three years is entirely used in construction activities, the total effect during the first year generates an increase of over R1.3 trillion in the income of all production activities and R250 billion of household income. These are implausibly large numbers within the context of the South African economy. From the results it is clear that a “large” infrastructural investment program is highly recommended. Though our analysis does not say anything about the size of such an investment the proposed R787 billion government infrastructural program is more than sufficient to generate the desired stimulus in the economy given the size of the multipliers in the construction sector. The path analysis which allowed us to get a better sense of the sectorial distributions of output, employment and household income tells us that benefits of this intervention will be distributed relatively evenly across the economy. The income generated creates significant economic influence that is propagated throughout the economy through various paths that reach all households through production activities that are directly and indirectly related to the infrastructure programme. Within production activities, business services, non-metallic metal products, mining and metal products are some of the most important sectors through which income is transmitted to households via factor payments. It is the sheer size of the proposed expenditure that leads to the large effects. It can be argued that, our analysis shows that government could get away with a smaller stimulus in the construction sector precisely because the multiplier effects are both large and reasonably well targeted. In addition, it should be pointed out that multiplier effects are not the only criterion for evaluating infrastructure spending. Even in the context of an economic downturn, the availability of useful projects is another important criterion. It would be unwise to explicitly or implicitly support infrastructure spending on white elephants because of demand side spillovers.

The distribution of benefits across households is not as favourable as one might like, with lower income households receiving only a fourth of the stimulus when compared to middle or upper income households. However, this is more a feature of the South African economy than of the construction sector as relatively few sectors provide a greater stimulus to overall household income than construction and even fewer provide a larger stimulus to lower income households.

Due to the economic downturn, most of these sectors are likely to be characterized by significant excess capacity. This implies that a demand injection into construction for infrastructure spending may be particularly well directed in terms of a stimulus to aggregate demand. A potential exception is business services where the effects of the contraction to date have been less pronounced.

Based on our results, the planned infrastructure programme has the potential to significantly offset the contractionary effects of the global downturn. The construction sector is an excellent choice for demand injection because it is large and



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thus able to accommodate a significant stimulus, it stimulates all other production activities and households at all income levels, and it results in infrastructure which should provide an improved foundation for growth into the future.

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**Table 5 – Structural Path Analysis: Selected Activities**

(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
Case	Origin	Destination	Global Influence	Path	Direct Influence	Path Multiplier	Total Influence	Accumulated Proportion
I	CCONS.	CIRON.	0.09	CCONS. CMETP. CIRON.	0.0174	1.64	0.0286	33.1
				CCONS. CIRON.	0.0156	1.50	0.0234	27.1
				CCONS. CELMA. CIRON.	0.0025	1.72	0.0043	5.0
				CCONS. CNMMP. CIRON.	0.0023	1.62	0.0037	4.3
				CCONS. CMACH. CIRON.	0.0007	1.65	0.0011	1.3
				CCONS. CBUSS. CIRON.	0.0003	2.34	0.0007	0.9
				CCONS. CELMA. CMETP. CIRON.	0.0003	1.88	0.0006	0.7
				CCONS. COTHM. CIRON.	0.0003	1.70	0.0005	0.6
				CCONS. CNMMP. CMETP. CIRON.	0.0003	1.78	0.0005	0.5
				CCONS. CFURN. CIRON.	0.0002	1.52	0.0003	0.4
				CCONS. CMACH. CMETP. CIRON.	0.0002	1.80	0.0003	0.3
				II	CCONS.	CNFRM.	0.05	CCONS. CELMA. CNFRM.
CCONS. CMETP. CNFRM.	0.0037	1.93	0.0071					20.7
CCONS. CMETP. CIRON. CNFRM.	0.0005	2.13	0.0010					3.0
CCONS. CIRON. CNFRM.	0.0004	1.95	0.0008					2.4
CCONS. CNMMP. CNFRM.	0.0002	1.84	0.0003					0.9
CCONS. CMACH. CNFRM.	0.0001	1.87	0.0003					0.8
CCONS. CBUSS. CNFRM.	0.0001	2.66	0.0003					0.8
CCONS. CIRON. CMETP. CNFRM.	0.0001	2.13	0.0002					0.6
CCONS. CMETP. CELMA. CNFRM.	0.0001	2.21	0.0002					0.5
CCONS. CELMA. CIRON. CNFRM.	0.0001	2.23	0.0002					0.5
CCONS. CELMA. CMETP. CNFRM.	0.0001	2.21	0.0002					0.5
III	CCONS.	CMETP.	0.12					CCONS. CMETP.
				CCONS. CIRON. CMETP.	0.0015	1.64	0.0024	2.1
				CCONS. CELMA. CMETP.	0.0011	1.70	0.0019	1.6
				CCONS. CNMMP. CMETP.	0.0009	1.61	0.0014	1.2
				CCONS. CMACH. CMETP.	0.0006	1.63	0.0009	0.8
				CCONS. CBUSS. CMETP.	0.0004	2.32	0.0008	0.7
				CCONS. COTHM. CMETP.	0.0003	1.55	0.0005	0.4
				CCONS. CELMA. CIRON. CMETP.	0.0002	1.88	0.0005	0.4
				CCONS. CNMMP. CIRON. CMETP.	0.0002	1.78	0.0004	0.3
				CCONS. CWOOD. CMETP.	0.0002	1.92	0.0004	0.3
				CCONS. CGOLD. CMETP.	0.0002	1.49	0.0003	0.3
				IV	CCONS.	CMACH.	0.06	CCONS. CMACH.
CCONS. CNMMP. CMACH.	0.0017	1.55	0.0027					4.6
CCONS. CMETP. CMACH.	0.0013	1.63	0.0021					3.6
CCONS. COTHM. CMACH.	0.0009	1.49	0.0014					2.4
CCONS. CBUSS. CMACH.	0.0004	2.24	0.0010					1.7
CCONS. CELMA. CMACH.	0.0004	1.64	0.0006					1.1
CCONS. CNMMP. COTHM. CMACH.	0.0004	1.62	0.0006					1.0
CCONS. CGOLD. CMACH.	0.0004	1.43	0.0006					1.0
CCONS. FLABHI. HHDMWHI. CMACH.	0.0002	2.03	0.0004					0.8
CCONS. FLABLS. HHDMID. CMACH.	0.0002	1.93	0.0004					0.7
CCONS. CPETR. CMACH.	0.0002	1.63	0.0004					0.6
V	CCONS.	CELEG.	0.06					CCONS. CELEG.
				CCONS. CNMMP. CELEG.	0.0011	1.54	0.0017	2.8
				CCONS. FLABLS. HHDMID. CELEG.	0.0005	1.89	0.0010	1.7
				CCONS. CELMA. CNFRM. CELEG.	0.0004	2.10	0.0009	1.6
				CCONS. FLABLS. HHDLW. CELEG.	0.0005	1.59	0.0009	1.5
				CCONS. CMETP. CELEG.	0.0005	1.62	0.0009	1.4
				CCONS. CGOLD. CELEG.	0.0005	1.42	0.0007	1.2
				CCONS. FLABHI. HHDMID. CELEG.	0.0003	2.01	0.0007	1.1
				CCONS. COTHM. CELEG.	0.0005	1.48	0.0007	1.1
				CCONS. CMETP. CNFRM. CELEG.	0.0003	2.10	0.0006	1.1
				CCONS. FLABHI. HHDMWHI. CELEG.	0.0003	1.99	0.0005	0.9

**Table 6 – Structural Path Analysis: Factors**

(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)					
Case	Origin	Destination	Global Influence	Path	Direct Influence	Path Multiplier	Total Influence	Proportion	Accumulated Proportion				
I	CCONS.	FCAP.	0.70	CCONS. FCAP.	0.0904	1.65	0.1489	21.3	21.3				
				CCONS. CBUSS. FCAP.	0.0177	2.34	0.0414	5.9	27.2				
				CCONS. CNMMP. FCAP.	0.0177	1.78	0.0316	4.5	31.7				
				CCONS. CBUSS. CFINS. FCAP.	0.0087	2.39	0.0207	3.0	34.7				
				CCONS. COTHM. FCAP.	0.0093	1.70	0.0159	2.3	36.9				
				CCONS. CMETP. FCAP.	0.0041	1.87	0.0076	1.1	38.0				
				CCONS. CNMMP. COTHM. FCAP.	0.0036	1.83	0.0067	1.0	39.0				
				CCONS. CELEG. FCAP.	0.0037	1.77	0.0065	0.9	39.9				
				CCONS. CAGRI. FCAP.	0.0031	1.80	0.0055	0.8	40.7				
				CCONS. CCOMM. FCAP.	0.0024	2.25	0.0055	0.8	41.5				
				CCONS. CPETR. FCAP.	0.0030	1.83	0.0054	0.8	42.3				
				II	CCONS.	FLABLS.	0.16	CCONS. FLABLS.	0.0556	1.40	0.0777	49.0	49.0
								CCONS. CMETP. FLABLS.	0.0033	1.59	0.0053	3.3	52.3
CCONS. CNMMP. FLABLS.	0.0032	1.51	0.0048					3.0	55.3				
CCONS. COTHM. FLABLS.	0.0033	1.45	0.0048					3.0	58.3				
CCONS. CGOLD. FLABLS.	0.0028	1.40	0.0040					2.5	60.8				
CCONS. CWOOD. FLABLS.	0.0018	1.80	0.0032					2.0	62.8				
CCONS. CELMA. FLABLS.	0.0019	1.60	0.0030					1.9	64.7				
CCONS. CNMMP. COTHM. FLABLS.	0.0013	1.57	0.0020					1.3	66.0				
CCONS. CPLAS. FLABLS.	0.0006	1.59	0.0010					0.6	66.6				
CCONS. CAGRI. FLABLS.	0.0005	1.55	0.0008					0.5	67.1				
CCONS. CPETR. COTHM. FLABLS.	0.0004	1.61	0.0006					0.4	67.5				
III	CCONS.	FLABSK.	0.20					CCONS. FLABSK.	0.0256	1.53	0.0393	19.4	19.4
								CCONS. CBUSS. CFINS. FLABSK.	0.0040	2.32	0.0093	4.6	23.9
				CCONS. CBUSS. FLABSK.	0.0025	2.27	0.0057	2.8	26.8				
				CCONS. CMETP. FLABSK.	0.0025	1.75	0.0043	2.1	28.9				
				CCONS. CNMMP. FLABSK.	0.0017	1.66	0.0029	1.4	30.3				
				CCONS. CWOOD. FLABSK.	0.0012	1.97	0.0024	1.2	31.5				
				CCONS. CELMA. FLABSK.	0.0012	1.75	0.0022	1.1	32.6				
				CCONS. COTHP. FLABSK.	0.0012	1.68	0.0021	1.0	33.6				
				CCONS. COTHM. FLABSK.	0.0011	1.59	0.0018	0.9	34.5				
				CCONS. CCOMM. FLABSK.	0.0007	2.11	0.0015	0.8	35.2				
				CCONS. CGOLD. FLABSK.	0.0006	1.53	0.0009	0.5	35.7				
				IV	CCONS.	FLABHL.	0.26	CCONS. FLABHL.	0.0445	1.58	0.0702	26.8	26.8
								CCONS. CBUSS. FLABHL.	0.0047	2.30	0.0108	4.1	30.9
CCONS. CBUSS. CFINS. FLABHL.	0.0029	2.36	0.0069					2.6	33.6				
CCONS. CNMMP. FLABHL.	0.0032	1.71	0.0055					2.1	35.6				
CCONS. CELMA. FLABHL.	0.0030	1.80	0.0053					2.0	37.7				
CCONS. CMETP. FLABHL.	0.0025	1.80	0.0044					1.7	39.4				
CCONS. COTHP. FLABHL.	0.0019	1.71	0.0033					1.3	40.6				
CCONS. CELEG. FLABHL.	0.0016	1.70	0.0028					1.1	41.7				
CCONS. COTHM. FLABHL.	0.0015	1.63	0.0025					1.0	42.6				
CCONS. CWOOD. FLABHL.	0.0008	2.03	0.0015					0.6	43.2				
CCONS. CPLAS. FLABHL.	0.0007	1.79	0.0013					0.5	43.7				

*The Economic Influence of Infrastructural Expenditure*  
*A Multiplier Decomposition and Structural Path Analysis*

**Table 7 – Structural Path Analysis: Institutions**

(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)					
Case	Origin	Destination	Global Influence	Path	Direct Influence	Path Multiplier	Total Influence	Proportion	Accumulated Proportion				
I	CCONS.	HENTRP.	0.65	CCONS. FCAP. HENTRP.	0.0834	1.65	0.1373	21.3	21.3				
				CCONS. CBUSS. FCAP. HENTRP.	0.0163	2.34	0.0382	5.9	27.2				
				CCONS. CNMMP. FCAP. HENTRP.	0.0163	1.78	0.0291	4.5	31.7				
				CCONS. COTHM. FCAP. HENTRP.	0.0086	1.70	0.0146	2.3	34.0				
				CCONS. CMETP. FCAP. HENTRP.	0.0037	1.87	0.0070	1.1	35.1				
				CCONS. CELEG. FCAP. HENTRP.	0.0034	1.77	0.0060	0.9	36.0				
				CCONS. CAGRI. FCAP. HENTRP.	0.0028	1.80	0.0051	0.8	36.8				
				CCONS. CCOMM. FCAP. HENTRP.	0.0022	2.25	0.0050	0.8	37.6				
				CCONS. CPETR. FCAP. HENTRP.	0.0027	1.83	0.0050	0.8	38.3				
				CCONS. CELMA. FCAP. HENTRP.	0.0025	1.88	0.0048	0.7	39.1				
				CCONS. CGOLD. FCAP. HENTRP.	0.0028	1.65	0.0046	0.7	39.8				
				II	CCONS.	HHDLow.	0.11	CCONS. FLABLS. HHDLow.	0.0174	1.47	0.0257	23.2	23.2
								CCONS. FLABSK. HHDLow.	0.0039	1.60	0.0063	5.7	28.9
CCONS. FCAP. HENTRP. HHDLow.	0.0028	1.73	0.0048					4.4	33.2				
CCONS. FLABHI. HHDLow.	0.0014	1.68	0.0024					2.2	35.4				
CCONS. CMETP. FLABLS. HHDLow.	0.0010	1.68	0.0017					1.6	37.0				
CCONS. CNMMP. FLABLS. HHDLow.	0.0010	1.59	0.0016					1.4	38.4				
CCONS. COTHM. FLABLS. HHDLow.	0.0010	1.52	0.0016					1.4	39.8				
CCONS. CGOLD. FLABLS. HHDLow.	0.0009	1.47	0.0013					1.2	41.0				
CCONS. CWOOD. FLABLS. HHDLow.	0.0006	1.90	0.0011					1.0	41.9				
CCONS. CELMA. FLABLS. HHDLow.	0.0006	1.68	0.0010					0.9	42.8				
CCONS. CBUSS. FLABSK. HHDLow.	0.0004	2.35	0.0009					0.8	43.6				
III	CCONS.	HHDMID.	0.42					CCONS. FLABLS. HHDMID.	0.0292	1.77	0.0517	12.4	12.4
								CCONS. FLABHI. HHDMID.	0.0190	1.88	0.0356	8.5	20.9
				CCONS. FCAP. HENTRP. HHDMID.	0.0141	1.95	0.0275	6.6	27.5				
				CCONS. FLABSK. HHDMID.	0.0143	1.82	0.0261	6.3	33.7				
				CCONS. CBUSS. FLABHI. HHDMID.	0.0020	2.60	0.0052	1.2	35.0				
				CCONS. CBUSS. FLABSK. HHDMID.	0.0014	2.56	0.0036	0.9	35.8				
				CCONS. CMETP. FLABLS. HHDMID.	0.0017	2.01	0.0035	0.8	36.7				
				CCONS. CNMMP. FLABLS. HHDMID.	0.0017	1.91	0.0032	0.8	37.4				
				CCONS. COTHM. FLABLS. HHDMID.	0.0017	1.82	0.0031	0.8	38.2				
				CCONS. CMETP. FLABSK. HHDMID.	0.0014	2.07	0.0028	0.7	38.9				
				CCONS. CNMMP. FLABHI. HHDMID.	0.0014	2.03	0.0028	0.7	39.5				
				IV	CCONS.	HHDWHL.	0.42	CCONS. FCAP. HENTRP. HHDWHL.	0.0249	1.87	0.0466	11.2	11.2
								CCONS. FLABHI. HHDWHL.	0.0239	1.86	0.0444	10.7	21.9
CCONS. FLABLS. HHDWHL.	0.0089	1.81	0.0162					3.9	25.7				
CCONS. FLABSK. HHDWHL.	0.0073	1.90	0.0138					3.3	29.1				
CCONS. CBUSS. FLABHI. HHDWHL.	0.0025	2.53	0.0064					1.5	30.6				
CCONS. CNMMP. FLABHI. HHDWHL.	0.0017	2.01	0.0034					0.8	31.4				
CCONS. CELMA. FLABHI. HHDWHL.	0.0016	2.12	0.0034					0.8	32.2				
CCONS. CMETP. FLABHI. HHDWHL.	0.0013	2.11	0.0028					0.7	32.9				
CCONS. COTHM. FLABHI. HHDWHL.	0.0010	1.96	0.0020					0.5	33.4				
CCONS. CBUSS. FLABSK. HHDWHL.	0.0007	2.56	0.0018					0.4	33.8				
CCONS. CELEG. FLABHI. HHDWHL.	0.0009	1.99	0.0017					0.4	34.2				

Figure 1 – Construction: Structural Path to all Institutions<sup>1</sup>

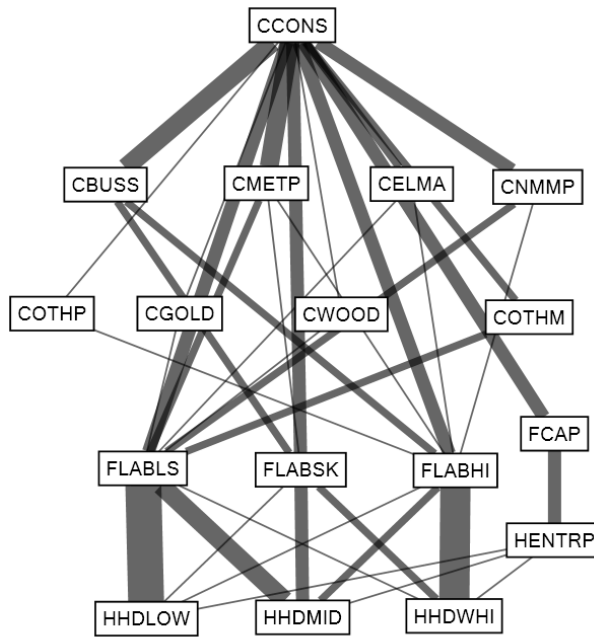
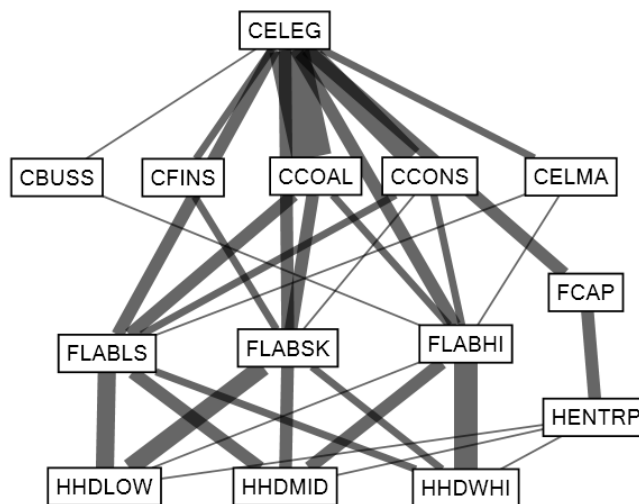
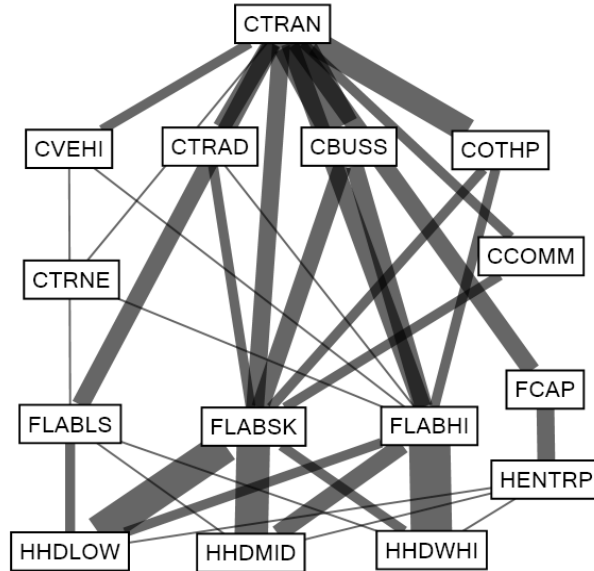


Figure 2 – Electricity and Gas: Structural Path to all Institutions



<sup>1</sup> All figures created using the weighted graph scheme of NodeXL.

**Figure 3 –Transportation: Structural Path to all Institutions**



**Figure 4 – Construction: Structural Path to Lower Income Households**

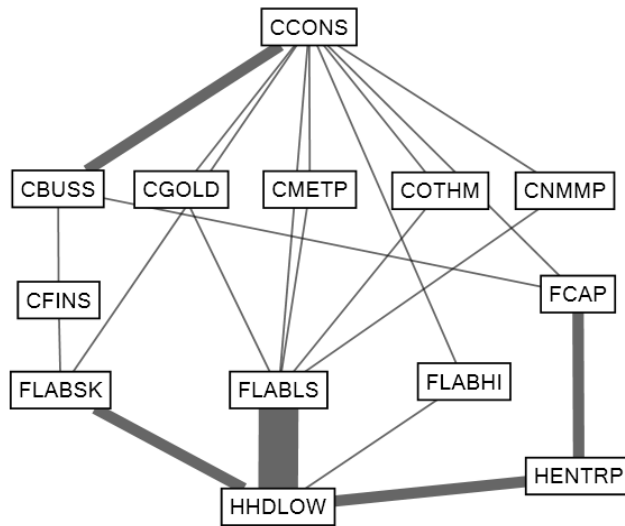


Figure 5 – Construction: Structural Path to Middle Income Households

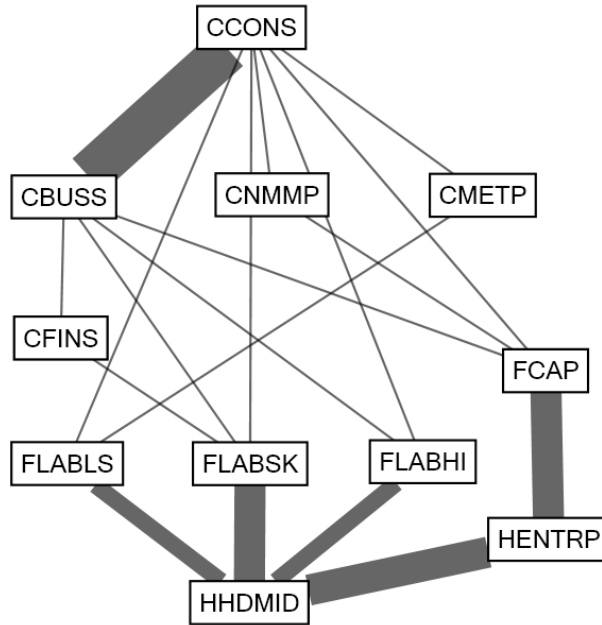
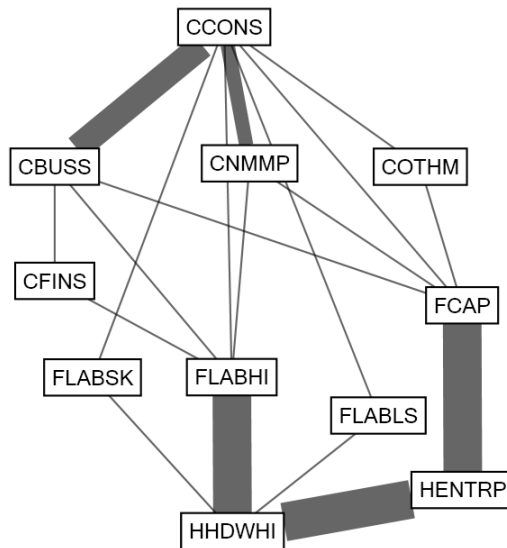


Figure 6 – Construction: Structural Path to Higher Income Households





## **6. Annex A: SAM Household Classification**

This study used a SAM where households were classified by income. Income level (e.g. division by income deciles) has sometimes been avoided as a classification criterion, because households are potentially mobile between income groups making ex ante and ex post comparisons and policy-targeting difficult (Pyatt and Thorbecke, 1976). Many different criteria have been attempted; however, three main criteria appear important in classifying households: a) location; b) resource endowment and wealth; and c) occupation of the head of the household. Location, particularly between rural and urban areas, is a crucial criterion largely on the grounds that policy often has a locational element and often an urban bias. Resource endowment is important at several levels. Access to land is a critical consideration in rural areas and the landless can be affected quite differently from the smallholder, or large farmers, by development policy. Likewise, the better educated in both the urban and rural areas are able to land jobs in formal and organized activities, whereas the uneducated are limited to employment opportunities largely in traditional agriculture and informal urban activities. The endowment of land and human capital is a crucial determinant of the ultimate income distribution and standards of living of the various socioeconomic household groups. It is with these considerations in mind that future work should try and use a classification that is in line with the above three criteria.